

### Method 4: Quadratic Formula

$$ax^2 + bx + c = 0 \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x^2 + 4x + 1 = 0$$

$a=1 \quad b=4 \quad c=1$

$$x = \frac{-(4) \pm \sqrt{(4)^2 - 4(1)(1)}}{2(1)}$$

$$= \frac{-4 \pm \sqrt{16-4}}{2} = \frac{-4 \pm \sqrt{12}}{2}$$

$$\frac{2\sqrt{3}}{\sqrt{4 \cdot 3}}$$

$$= \frac{-4 \pm 2\sqrt{3}}{2}$$

$$= -\frac{4}{2} \pm \frac{2\sqrt{3}}{2}$$

$$x = -2 \pm \sqrt{3}$$

$$x = -2 + \sqrt{3}, -2 - \sqrt{3}$$

### Method 5: Complex Solutions

$$x^2 + 9 = 0$$

$$x^2 = -9$$

$$x^2 - 9 = 0$$

$$(x+3)(x-3) = 0$$

$$x = \pm \sqrt{-9}$$

$$= \pm \sqrt{9} \sqrt{-1}$$

$$= \pm 3i$$

$$x = \pm 3i \quad \text{or} \quad x = 3i, -3i$$

### Method 6: Rational Exponents (Fractions)

$$2x^{3/2} + 5 = 133$$

$$2x^{3/2} = 128$$

$$2x + 5 = 133$$

$$2x = 128$$

$$x^{3/2} = \frac{128}{2}$$

$$x^{3/2} = 64$$

$$x = \frac{128}{2}$$

$$x = 64$$

$$x^{3/2} = 64$$

$$(x^{3/2})^{2/3} = (64)^{2/3}$$

\* raise both sides to the reciprocal exponent

$$X^{3/2} = 64$$

$$\sqrt{x^3} = 64^2$$

$$\sqrt[3]{x^3} = \sqrt[3]{4096}$$

$$x = 16$$

$$(x^{3/2})^{-1} = (64)^{-1}$$

\* raise both sides to the reciprocal exponent

$$x = 64^{2/3} = \sqrt[3]{64^2} = \sqrt[3]{4096}$$

$$x = 16$$

$$x^{A/B} = \sqrt[B]{x^A}$$