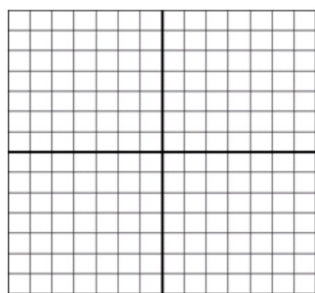
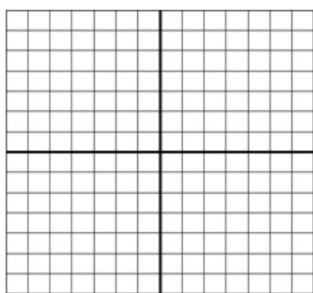


Determine the domain of the following functions. Draw a sketch of the graph.

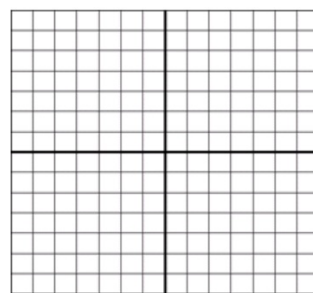
1.  $y = \frac{1}{x}$



2.  $y = \frac{1}{x-2}$



3.  $y = \frac{x^2 - 4}{x - 2}$



## Discontinuities

### Holes

(removable discontinuity)

- occur when there is a value of  $x$  that makes the denominator equal to zero, but we can cancel out the factor

1. Set the canceled factor equal to 0.

2. Solve for  $x$ .

3. Plug the answer into the simplified equation to get  $y$ .

4.  $(x, y)$  is the hole

Examples of functions with holes:

1.  $f(x) = \frac{x+2}{x^2-4}$

2.  $g(x) = \frac{x+3}{x^2-2x-15}$

### Vertical Asymptotes

(non-removable discontinuity)

- occur when there is a value of  $x$  that would make the denominator equal to zero, but we can't get rid of the factor

Examples of functions with vertical asymptotes:

1.  $y = \frac{x}{2x-6}$

2.  $y = \frac{10}{x^2-4}$

3.  $y = \frac{x+5}{x^3+5x^2+6x}$

**Horizontal Asymptote** - occur in 2 out of the 3 cases

- to find a horizontal asymptote, examine what happens to the function as  $x$  approaches infinity

**Conclusion (short cut)**

Case 1:

→ Denominator exponent is larger/higher

Case 2:

→ Exponents are equal

Case 3:

→ Numerator exponent is larger/higher

1.  $y = \frac{1}{x+1}$

2.  $y = \frac{5x^2 + 4x}{x^2 - 7}$

3.  $y = \frac{x^3 - 2}{x^2 - 4}$

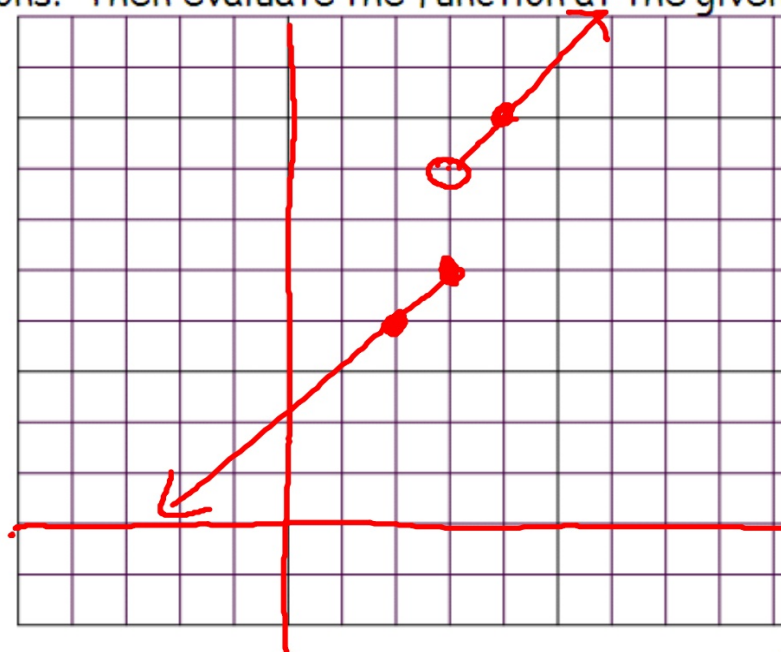
Plot the following piecewise functions. Then evaluate the function at the given

$$f(x) = \begin{cases} x + 2 & \text{if } x \leq 3 \\ x + 4 & \text{if } x > 3 \end{cases}$$

$$f(0) = 2$$

$$f(3) = 5$$

$$f(-2) = 0$$



$$f(x) = \begin{cases} x^2 & \text{if } x > 1 \\ 2 & \text{if } x \leq 1 \end{cases}$$

$$\begin{aligned} &= 2 \\ &) = 9 \\ &2) = 2 \end{aligned}$$



$$f(x) = \begin{cases} 2 & \text{if } x \leq -1 \\ -x+1 & \text{if } -1 < x < 1 \\ \frac{1}{2}x - \frac{1}{2} & \text{if } x \geq 1 \end{cases}$$

$$f(0) = 1 \quad f(3) = 1$$

$$f(0) = 0 \quad f\left(\frac{1}{2}\right) = \frac{1}{2}$$

$$f(-1) = 2 \quad f(-2) = 2$$

