

Find $\frac{dy}{dx}$.

1) $4x^2y - 3y = x^3 - 1$

Method of Separating Variables:

Find $\frac{dy}{dx}$.

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Method of Implicit Differentiation:

Implicit Differentiation:

taking the derivative when there are multiple variables

$$2) y^3 + 7y = x^3$$

$$3) 1 = x^2 y + y$$

$$0 = 2xy + x^2 \cdot \frac{dy}{dx} + 1 \frac{dy}{dx}$$

$$-2xy = \frac{dy}{dx} (x^2 + 1)$$

$$\frac{-2xy}{x^2 + 1} = \frac{dy}{dx}$$

$$4) 4x^3 + 5xy^2 - 2y^2 = 6$$

$$12x^2 + 5y^2 + 5x \cdot 2y \frac{dy}{dx} - 4y \frac{dy}{dx} = 0$$

$$10xy \frac{dy}{dx} - 4y \frac{dy}{dx} = -12x^2 - 5y^2$$

$$\frac{dy}{dx} (10xy - 4y) = -12x^2 - 5y^2$$

$$\frac{dy}{dx} = \frac{-12x^2 - 5y^2}{10xy - 4y}$$

$$5) y^3 - xy^2 + \cos(xy) = 2$$

$$3y^2 \frac{dy}{dx} - 1y^2 + -x \cdot 2y \frac{dy}{dx} + -\sin(xy)(1 \cdot y + x \frac{dy}{dx})$$

$$\boxed{3y^2 \frac{dy}{dx}} - y^2 - \boxed{2xy \frac{dy}{dx}} - \sin(xy)(y + x \frac{dy}{dx}) = 0$$

$$\frac{dy}{dx} (3y^2 - 2xy) = \sin(xy)(y + x \frac{dy}{dx}) + y^2$$

