

Section 3.5 Notes: Exponential and Logarithmic Models

Population Formula: $A = I r^t$

1.) The population of a town in 2015 is 134,000. It has an annual rate of increase of 5.7%.

a.) What is the growth rate? 1.057

b.) Create a formula for the population growth. $A = 134,000(1.057)^t$

c.) Based on this growth, what is the expected population in 2020? $A = 134,000(1.057)^5 =$

$$A = 176,799$$

2.) The population of a town in 2002 is 78,000. It has an annual rate of decrease of 5.7%.

a.) What is the growth rate? $1 - .057 = .943$

b.) Create a formula for the population growth. $A = 78,000(.943)^t$

c.) Based on this growth, what is the expected population in 2020?

$$A = 78,000(.943)^{18} =$$

$$A = 27,120$$

3.) The population of a town in 2005 is 27,500. It has an annual rate of increase of 2.5%.

a.) What is the growth rate? 1.025

b.) Create a formula for the population growth. $A = 27,500(1.025)^t$

c.) Based on this growth, what is the expected population in 2025?

$$A = 27,500(1.025)^{20} =$$

$$A = 45,040$$

4.) The population of a town in 2012 is 123,000. It has an annual rate of decrease of 2.7%.

a.) What is the growth rate? $1 - .027 = .973$

b.) Create a formula for the population growth. $A = 123,000(.973)^t$

c.) Based on this growth, what is the expected population in 2017?

$$A = 123,000(.973)^5 =$$

$$A = 107,268$$

$$F_n = p \left[\frac{(1+i)^n - 1}{i} \right]$$

$$P_n = p \left[\frac{1 - (1+i)^{-n}}{i} \right]$$

5. You decide to put away \$200 a month into your 401K. You expect to see a 5% return on average. If you plan to retire after 40 years of working, how much will your 401K be worth?

$$F_n = 200 \left[\frac{\left(1 + \frac{.05}{12}\right)^{480} - 1}{\left(\frac{.05}{12}\right)} \right] = \boxed{\$305,204.03}$$

1526.020156

\$96,000 Put in

6. You decide to put away \$250 a month into your 401K. You expect to see a 5% return on average. If you plan to retire after 35 years of working, how much will your 401K be worth?

$$F_n = 250 \left[\frac{\left(1 + \frac{.05}{12}\right)^{420} - 1}{\left(\frac{.05}{12}\right)} \right] = \boxed{\$284,023.11}$$

\$105,000 Put in

7. You have found a car for \$18,000. The dealership has offered you a 5.5% interest rate for a 6 year loan. What is your monthly payment on your loan?

$$18,000 = p \left[\frac{1 - \left(1 + \frac{.055}{12}\right)^{-72}}{\left(\frac{.055}{12}\right)} \right] = \boxed{\$294.08}$$

8. You have found a car for \$18,000. The dealership has offered you a 5% interest rate for a 5 year loan. What is your monthly payment on your loan?

$$18,000 = p \left[\frac{1 - \left(1 + \frac{.05}{12}\right)^{-60}}{\left(\frac{.05}{12}\right)} \right] = \boxed{\$339.68}$$