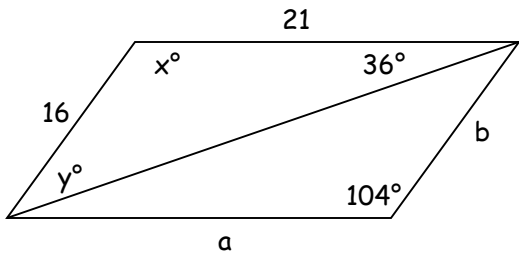


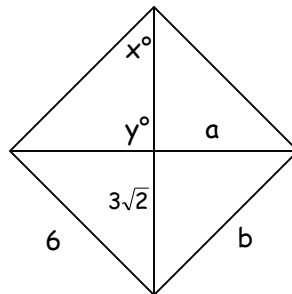
For each problem (1-4) a and b are segment lengths; x and y are angle measures.

1. Figure is a Parallelogram



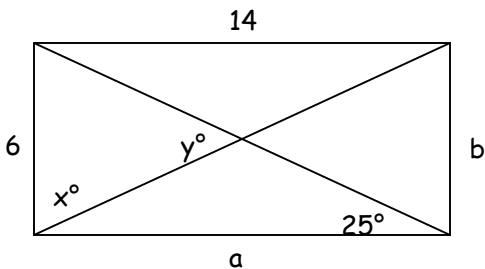
$$\begin{aligned} a &= 21 \\ b &= 16 \\ x &= 104 \\ y &= 40 \end{aligned}$$

2. Figure is a Square



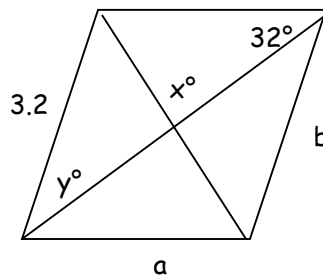
$$\begin{aligned} a &= 3\sqrt{2} \\ b &= 6 \\ x &= 45 \\ y &= 90 \end{aligned}$$

3. Figure is a Rectangle



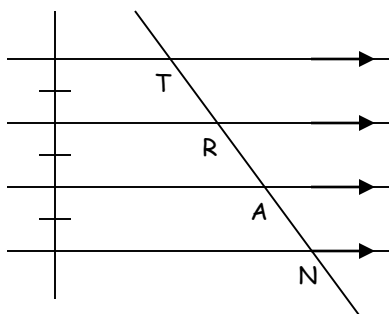
$$\begin{aligned} a &= 14 \\ b &= 6 \\ x &= 65 \\ y &= 50 \end{aligned}$$

4. Figure is a Rhombus



$$\begin{aligned} a &= 3.2 \\ b &= 3.2 \\ x &= 90 \\ y &= 32 \end{aligned}$$

5.  $TR + TR = RN$   
 $2x + 2x = 5x - 9$   
 $4x = 5x - 9$   
 $-x = -9$   
 $x = 9$



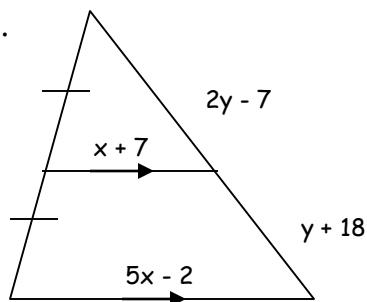
6.  $TA = RN$   
 $4x + 9 = 9x + 6$   
 $3 = 5x$   
 $x = 3/5$

5. If  $TR = 2x$  and  $RN = 5x - 9$ , then  $x = 9$ .

6. If  $TA = 4x + 9$  and  $RN = 9x + 6$ , then  $x = 3/5$ .

7. If  $TA = 16$ , then  $TN = 24$ . (Each piece is 8).

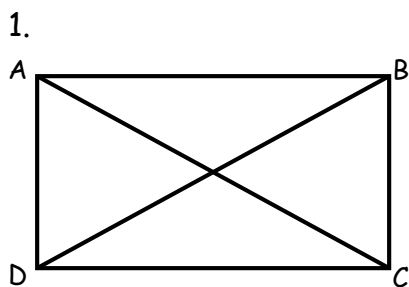
8.



$$\begin{aligned} 2y - 7 &= y + 18 \\ y &= 25 \end{aligned}$$

$$\begin{aligned} x + 7 + x + 7 &= 5x - 2 \\ 2x + 14 &= 5x - 2 \\ 16 &= 3x \\ x &= 16/3 \end{aligned}$$

$$\begin{aligned} x &= 16/3 \\ y &= 25 \end{aligned}$$



ABCD is a rectangle

$$AC = x^2$$

$$BD = x + 72$$

$$x^2 = x + 72$$

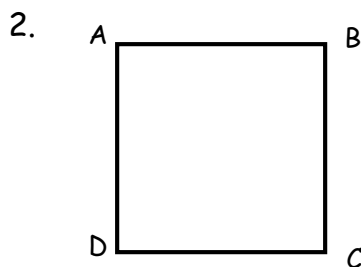
$$x^2 - x - 72 = 0$$

$$(x - 9)(x + 8) = 0$$

$$x = 9, x = -8$$

$$x = 9$$

$$x = -8$$



ABCD is a square

$$m\angle DAB = 4x + 4y$$

$$m\angle ADC = 8x - 4y$$

$$4x + 4y = 90$$

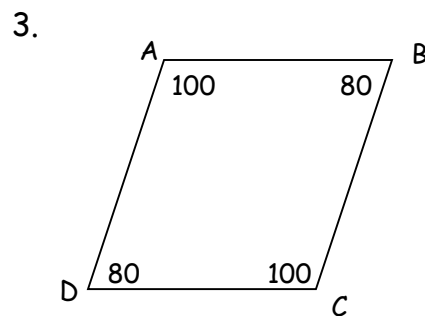
$$8x - 4y = 90$$

$$12x = 180 \quad x = 15$$

$$4(15) + 4y = 90$$

$$4y = 30 \quad x = 15$$

$$y = 7.5 \quad y = 7.5$$



ABCD is a rhombus

$$m\angle DAB = 15y - 35$$

$$m\angle DCB = 20x$$

$$m\angle ADC = 80$$

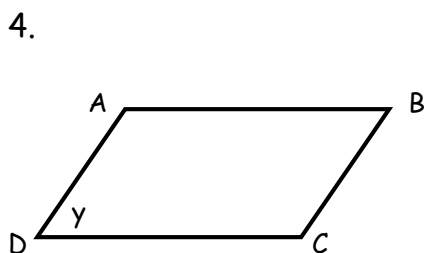
$$15y - 35 = 100$$

$$15y = 135$$

$$y = 9$$

$$20x = 100 \quad x = 5$$

$$x = 5 \quad y = 9$$



ABCD is a parallelogram

$$m\angle A = 5x + 9$$

$$m\angle B = 7x + 3$$

$$5x + 9 + 7x + 3 = 180$$

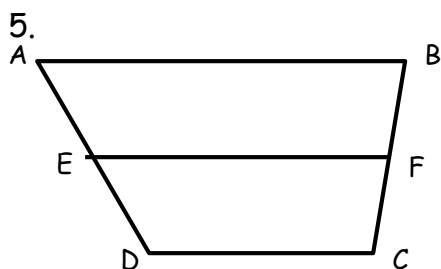
$$12x + 12 = 180$$

$$12x = 168$$

$$x = 14$$

$$x = 14$$

$$y = 101$$



ABCD is a trapezoid; EF is the median

$$AE = 5x - 7 \quad BF = y^2$$

$$AD = 6x + 2 \quad FC = -y + 6$$

$$AE + AE = AD$$

$$5x - 7 + 5x - 7 = 6x + 2$$

$$10x - 14 = 6x + 2$$

$$4x = 16$$

$$x = 4$$

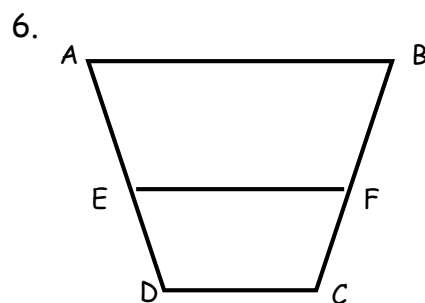
$$y^2 = -y + 6$$

$$y^2 + y - 6 = 0$$

$$(y + 3)(y - 2) = 0 \quad x = 4$$

$$y + 3 = 0; y = -3 \quad y = -3$$

$$y - 2 = 0; y = 2 \quad y = 2$$



ABCD is an isosceles trapezoid

EF is the median

$$AB = 8x - 2$$

$$EF = 3x + 7$$

$$DC = 3x + 6$$

$$\frac{AB + DC}{2} = EF$$

$$\frac{8x - 2 + 3x + 6}{2} = 3x + 7$$

$$11x + 4 = 6x + 14$$

$$5x = 10$$

$$x = 2$$

$$x = 2$$

Property	Parallelogram	Rectangle	Rhombus	Square
All angles are right angles		x		x
Both Pairs of Opposite sides are parallel	x	x	x	x
All sides are congruent			x	x
Both Pairs of Opposite angles are congruent	x	x	x	x
Diagonals bisect interior angles of quadrilateral			x	x
Diagonals are perpendicular			x	x
Diagonals are congruent		x		x
Diagonals bisect one another	x	x	x	x
Both Pairs of Opposite sides are congruent	x	x	x	x

True and False

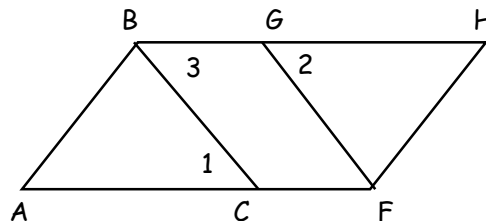
- False 1. All quadrilaterals are parallelograms.
- True 2. All parallelograms are quadrilaterals.
- True 3. All squares are rhombi.
- True 4. All rectangles are parallelograms.
- False 5. If a parallelogram has  $\perp$  diagonals and four congruent sides it must be a square.
- False 6. If diagonals of a quadrilateral are congruent, then the quadrilateral is a parallelogram.
- False 7. An isosceles trapezoid has two congruent bases.
- True 8. If diagonals of a quadrilateral bisect one another, then the quadrilateral is a parallelogram.
- False 9. All trapezoids are parallelograms.
- False 10. All parallelograms are rectangles.
- True 11. If both pairs of opposite angles of a quadrilateral are congruent, then the quadrilateral is a parallelogram.
- True 12. All trapezoids are quadrilaterals.
- False 13. If one pair of opposite sides in a quadrilateral are parallel, then the quadrilateral is a parallelogram.
- False 14. All rhombi are squares.
- True 15. The sum of the interior angles of a trapezoid is 360.
- True 16. A square has congruent diagonals.
- False 17. A trapezoid can have four congruent sides.
- False 18. The diagonals of a rhombus are always congruent.
- True 19. If one pair of opposite sides in a quadrilateral are parallel and congruent, then the quadrilateral is a parallelogram.
- False 20. All rectangles have perpendicular diagonals.
- True 21. Diagonals of a rhombus bisect one another.
- True 22. An isosceles trapezoid has congruent legs.
- True 23. A trapezoid can have no congruent sides.
- False 24. The legs of a trapezoid are parallel.
- False 25. If two lines have equal slopes, then the lines are perpendicular.

Complete the blank with the word always, sometimes or never.

1. A square is ALWAYS a rhombus.
2. The diagonals of a parallelogram ALWAYS bisect one another.
3. A parallelogram with four congruent sides is SOMETIMES a rectangle.
4. The diagonals of a rhombus are SOMETIMES congruent.
5. A rectangle ALWAYS has opposite sides that are congruent.
6. A parallelogram SOMETIMES has perpendicular diagonals.
7. A rectangle is SOMETIMES a square.
8. A square is ALWAYS a rectangle.
9. A parallelogram ALWAYS has opposite congruent angles.
10. A rhombus is SOMETIMES a rectangle.
11. A rhombus ALWAYS has perpendicular diagonals.
12. A trapezoid is NEVER a parallelogram.
13. A rectangle ALWAYS has congruent diagonals.
14. A square ALWAYS has four congruent sides.
15. A parallelogram SOMETIMES congruent diagonals.
16. A parallelogram is SOMETIMES a square.
17. A rectangle SOMETIMES has perpendicular diagonals.
18. A rectangle is SOMETIMES a rhombus.
19. A trapezoid NEVER has two pairs of opposite parallel sides.
20. A square is ALWAYS a rhombus.
21. A rhombus is SOMETIMES a square.
22. A rhombus SOMETIMES has four right angles.
23. A parallelogram with congruent diagonals and four right angles is ALWAYS a rectangle.
24. Opposite sides of a parallelogram are ALWAYS congruent.
25. The legs of a trapezoid are SOMETIMES congruent.
26. A rhombus SOMETIMES has four congruent angles.
27. A parallelogram has interior angles that ALWAYS add up to  $360^\circ$ .
28. A square is NEVER a trapezoid.
29. The bases of a trapezoid are ALWAYS parallel.
30. A trapezoid is NEVER a rhombus.
31. A rhombus SOMETIMES has congruent diagonals.
32. A square is ALWAYS a parallelogram.
33. The legs of a trapezoid are NEVER parallel.
34. The bases of a trapezoid are NEVER congruent.

Given: BGCF is a parallelogram;  $AC \cong GH$

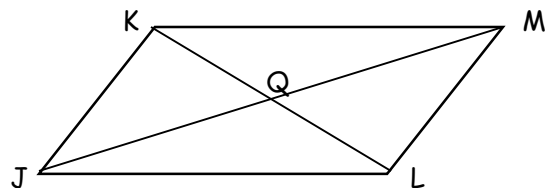
Prove:  $\angle A \cong \angle H$



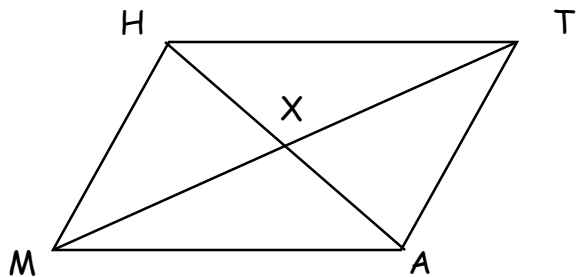
Statements	Reasons
1. BGCF is a parallelogram	1. Given
2. $BC \cong GF$	2. Opposite sides of a parallelogram are congruent.
3. $BC \parallel GF$ ; $BG \parallel CF$	3. Definition of a Parallelogram
4. $\angle 1 \cong \angle 3$	4. If two parallel lines are cut by a transversal, then alternate interior angles are congruent.
5. $\angle 3 \cong \angle 2$	5. If two parallel lines are cut by a transversal, then corresponding angles are congruent.
6. $\angle 1 \cong \angle 2$	6. Substitution
7. $AC \cong GH$	7. Given
8. $\triangle BAC \cong \triangle FHG$	8. SAS
9. $\angle A \cong \angle H$	9. CPCTC

Given:  $\triangle KQJ \cong \triangle LQM$

Prove: KMLJ is a parallelogram



Statements	Reasons
1. $\triangle KQJ \cong \triangle LQM$	1. Given
2. $\angle JKQ \cong \angle MLQ$	2. CPCTC
3. $KJ \parallel LM$	3. If two lines are cut by a transversal and alternate interior angles are congruent, then the lines are parallel.
4. $KJ \cong LM$	4. CPCTC
5. KMLJ is a parallelogram	5. If one pair of opposite sides of a quadrilateral are both parallel and congruent, then the quadrilateral is a parallelogram.



1.  $MA \cong TH$  and  $MH \cong AT$ : If both pairs of opposite sides are congruent, then the quadrilateral is a parallelogram.
2.  $MA \parallel TH$  and  $MA \cong TH$ : If one pair of opposite sides are both congruent and parallel, then the quadrilateral is a parallelogram.
3.  $TX \cong XM$  and  $AX \cong HX$ : If the diagonals bisect one another, then the quadrilateral is a parallelogram.
4.  $HM \cong AT$  and  $HT \parallel MA$ : NO
5.  $\angle MAT \cong \angle MHT$  and  $\angle HMA \cong \angle HTA$ : If both pairs of opposite angles are congruent, then the quadrilateral is a parallelogram.
6.  $\angle MXH \cong \angle TXA$  and  $\angle HMA \cong \angle HTA$ : NO
7. X is the midpoint of MT and HA: If the diagonals bisect one another, then the quadrilateral is a parallelogram.
8.  $\angle MHA \cong \angle HAT$  and  $\angle THA \cong \angle MAH$ : Because the pairs of alternate interior angles are congruent, you can conclude that the opposite sides are parallel - then: If both pairs of opposite sides of a quadrilateral are parallel, then the quadrilateral is a parallelogram. (OR Definition of a Parallelogram)
9.  $HA \cong MT$ : NO
10.  $\angle MHA \cong \angle HAT$  and  $HT \parallel MA$  Definition of a Parallelogram (Similar to #8)

Classify each figure as specifically as you can based on the markings in the diagram.

<p>1.</p> <p>Rectangle</p>	<p>2.</p> <p>Isosceles Trapezoid</p>	<p>3.</p> <p>Quadrilateral</p>
<p>4.</p> <p>Parallelogram</p>	<p>5.</p> <p>Parallelogram</p>	<p>6.</p> <p>Square</p>